

NAG Toolbox for MATLAB

c06fc

1 Purpose

c06fc calculates the discrete Fourier transform of a sequence of n complex data values (using a work array for extra speed).

2 Syntax

```
[x, y, ifail] = c06fc(x, y, 'n', n)
```

3 Description

Given a sequence of n complex data values z_j , for $j = 0, 1, \dots, n-1$, c06fc calculates their discrete Fourier transform defined by

$$\hat{z}_k = a_k + ib_k = \frac{1}{\sqrt{n}} \sum_{j=0}^{n-1} z_j \times \exp\left(-i \frac{2\pi jk}{n}\right), \quad k = 0, 1, \dots, n-1.$$

(Note the scale factor of $\frac{1}{\sqrt{n}}$ in this definition.)

To compute the inverse discrete Fourier transform defined by

$$\hat{w}_k = \frac{1}{\sqrt{n}} \sum_{j=0}^{n-1} z_j \times \exp\left(+i \frac{2\pi jk}{n}\right),$$

this function should be preceded and followed by calls of c06gc to form the complex conjugates of the z_j and the $\hat{z}_k$.

c06fc uses the fast Fourier transform (FFT) algorithm (see Brigham 1974). There are some restrictions on the value of n (see Section 5).

4 References

Brigham E O 1974 *The Fast Fourier Transform* Prentice-Hall

5 Parameters

5.1 Compulsory Input Parameters

1: **x(n) – double array**

If **x** is declared with bounds $(0 : n-1)$ in the (sub)program from which c06fc is called, then **x(j)** must contain x_j , the real part of z_j , for $j = 0, 1, \dots, n-1$.

2: **y(n) – double array**

If **y** is declared with bounds $(0 : n-1)$ in the (sub)program from which c06fc is called, then **y(j)** must contain y_j , the imaginary part of z_j , for $j = 0, 1, \dots, n-1$.

5.2 Optional Input Parameters

1: **n – int32 scalar**

Default: The dimension of the array **x**.

n , the number of data values. The largest prime factor of $\mathbf{n}$ must not exceed 19, and the total number of prime factors of $\mathbf{n}$, counting repetitions, must not exceed 20.

Constraint: $\mathbf{n} > 1$.

5.3 Input Parameters Omitted from the MATLAB Interface

work

5.4 Output Parameters

1: **$\mathbf{x}(\mathbf{n})$ – double array**

The real parts a_k of the components of the discrete Fourier transform. If $\mathbf{x}$ is declared with bounds $(0 : \mathbf{n} - 1)$ in the (sub)program from which c06fc is called, then for $0 \leq k \leq n - 1$, a_k is contained in $\mathbf{x}(k)$.

2: **$\mathbf{y}(\mathbf{n})$ – double array**

The imaginary parts b_k of the components of the discrete Fourier transform. If $\mathbf{y}$ is declared with bounds $(0 : \mathbf{n} - 1)$ in the (sub)program from which c06fc is called, then for $0 \leq k \leq n - 1$, b_k is contained in $\mathbf{y}(k)$.

3: **ifail – int32 scalar**

0 unless the function detects an error (see Section 6).

6 Error Indicators and Warnings

Errors or warnings detected by the function:

ifail = 1

At least one of the prime factors of $\mathbf{n}$ is greater than 19.

ifail = 2

$\mathbf{n}$ has more than 20 prime factors.

ifail = 3

On entry, $\mathbf{n} \leq 1$.

ifail = 4

An unexpected error has occurred in an internal call. Check all (sub)program calls and array dimensions. Seek expert help.

7 Accuracy

Some indication of accuracy can be obtained by performing a subsequent inverse transform and comparing the results with the original sequence (in exact arithmetic they would be identical).

8 Further Comments

The time taken is approximately proportional to $n \times \log n$, but also depends on the factorization of n . c06fc is faster if the only prime factors of n are 2, 3 or 5; and fastest of all if n is a power of 2.

9 Example



```
x = [0.34907;  
     0.548900000000000001;  
     0.74776;  
     0.94459;  
     1.1385;  
     1.3285;  
     1.5137];  
y = [-0.37168;  
     -0.35669;  
     -0.31175;  
     -0.23702;  
     -0.13274;  
     0.00074;  
     0.16298];  
[xOut, yOut, ifail] = c06fc(x, y)
```

```
xOut =  
    2.4836  
   -0.5518  
   -0.3671  
   -0.2877  
   -0.2251  
   -0.1483  
    0.0198  
yOut =  
   -0.4710  
    0.4968  
    0.0976  
   -0.0586  
   -0.1748  
   -0.3084  
   -0.5650  
ifail =  
      0
```